

RATIONAL NUMBER OPERATIONS

CHEAT SHEET - A

Name _____

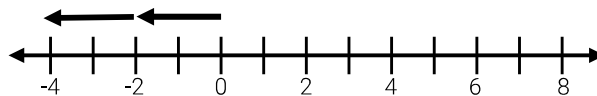
Date _____ Pd _____

ADDITION

- If the signs are the **SAME**, then **ADD** and use the same sign.
- If the signs are **DIFFERENT**, then **SUBTRACT** and **TAKE THE SIGN** of the number with the **GREATEST ABSOLUTE VALUE**.

$$-2 + -2 = -4$$

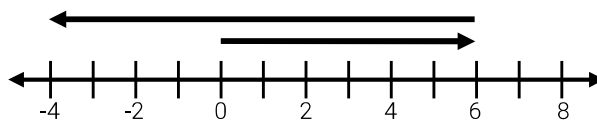
integers



SUBTRACTION

- Rewrite the problem to **ADD THE OPPOSITE**. Then, follow the rules for adding rational numbers.

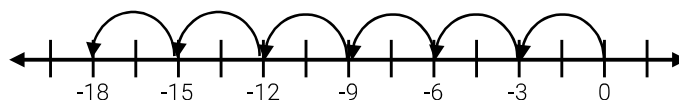
$$6 - 10 = -4$$



MULTIPLICATION & DIVISION

- If there is an **EVEN NUMBER** of signs, then the solution is **POSITIVE**.
- If there is an **ODD NUMBER** of signs, then the solution is **NEGATIVE**.

$$-3 \cdot 6 = -18$$



Integer Operations

$$8 - 11 = \underline{-3}$$

$$-3 - 13 = \underline{-16}$$

$$15 \div -3 = \underline{-5}$$

$$-4 + -6 = \underline{-10}$$

$$8 + -2 = \underline{6}$$

$$6 \cdot -9 = \underline{-54}$$

$$-27 \div 9 = \underline{-3}$$

$$8 \cdot 11 = \underline{88}$$

$$12 - (-9) = \underline{21}$$

Rational Number Operations

$$-9.6 \cdot 5 = -48$$

$$-60.8 \div 4 = -15.2$$

$$\frac{3}{5} \cdot \frac{1}{4} = \frac{3}{20}$$

$$\frac{5}{8} \div \frac{3}{4} = \frac{5}{6}$$

$$-12.7 \cdot -3 = 38.1$$

$$100 \div 2.5 = 40$$

$$\frac{2}{3} \cdot \frac{3}{2} = 1$$

$$\frac{4}{7} \div \frac{1}{2} = 1\frac{1}{7}$$

PROPORTIONALITY & SCALE DRAWINGS

Name _____

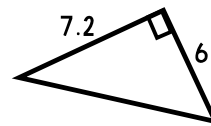
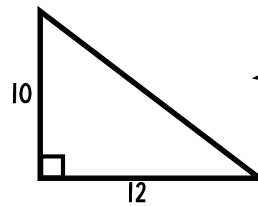
CHEAT SHEET - A

Date _____ Pd _____

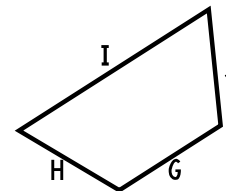
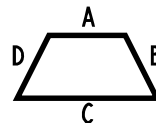
Similarity

SIMILAR FIGURES have **CORRESPONDING**:

1. **PROPORTIONAL** sides
2. **EQUAL** angles



$$\frac{10}{12} = \frac{6}{7.2}$$



$$\frac{A}{G} = \frac{B}{H}$$

Scale Factors

NEW
ORIGINAL

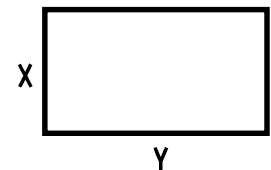
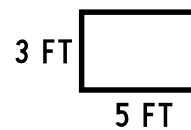
The **SCALE FACTOR** is the ratio in which a figure is **DILATED**.

ENLARGEMENT

REDUCTION

scale factor is greater than 1

scale factor is less than 1



SCALE FACTOR OF 1.5



$$X = 4.5 \text{ FT}$$

$$Y = 7.5 \text{ FT}$$

SCALE DRAWING: uses a **SCALE** to convert measurements

$$1 \text{ CM} = 2.5 \text{ MILES}$$

$$1 \text{ IN} = 300 \text{ FEET}$$

Frequently used on **MAPS** and **BLUEPRINTS**

- Label the various units
- The conversion will be given
- Set up and solve the proportion

Scale Drawings

$$\frac{\text{IN}}{\text{FT}} = \frac{2}{75} = \frac{7}{X}$$

$$525 = 2X$$

$$262.5 = X$$

$$7 \text{ IN} = 262.5 \text{ FT}$$

RATES AND PERCENTS

CHEAT SHEET - A

Name _____

Date _____ Pd _____

RATE: a ratio with **TWO DIFFERENT UNITS**

$$\frac{\$5.25}{6 \text{ LB}}$$

$$\frac{250 \text{ MI}}{4 \text{ HRS}}$$

$$\frac{49 \text{ FT}}{5 \text{ SEC}}$$

UNIT RATE: a ratio with a quantity of **ONE**

$$\frac{\text{PRICE}}{1 \text{ LB}}$$

$$\frac{\text{MILES}}{1 \text{ HR}}$$

$$\frac{\text{FEET}}{1 \text{ SEC}}$$

FRACTIONAL UNIT RATE

- Will result in a complex fraction
- Follow the steps for dividing fractions

$$\frac{\text{MILES}}{\text{HR}} = \frac{\frac{1}{3}}{\frac{1}{4}} = \frac{1}{3} \cdot \frac{4}{1} = \frac{4}{3}$$

$$1\frac{1}{3} \text{ MILES IN 1 HOUR}$$

rates

INTEREST & ERROR

SIMPLE INTEREST: $I = p \cdot r \cdot t$

I = interest

p = principal

r = annual interest rate (as a decimal)

t = time (in years)

- Be sure to change the rate to a decimal and convert any number of months to years.

PERCENT ERROR

$$\frac{|A-X|}{|X|} = \frac{\%}{100}$$

A = approximate

X = exact

PERCENT VOCABULARY

MARKUP

tax
tip
mark up
gratuity
increase

DISCOUNT

sale price
amount off
decrease
mark down
discount
whole sale

OTHER

commission
interest

PERCENT: a **QUANTITY** out of **100**

- Set up a percent proportion or an equation
- Solve for the missing quantity
- Reread the problem to make sure you answer the question

$$\frac{\%}{100} = \frac{\text{PART}}{\text{WHOLE}}$$

$$\text{PART} = \% \cdot \text{WHOLE}$$

(as a decimal)

PERCENT OF CHANGE: the percent **GAINED** or **LOST** over a period of time

- Determine the change
- Set up a percent proportion
- Solve for the missing quantity
- Reread the problem to make sure you answer the question

$$\frac{\%}{100} = \frac{\text{CHANGE}}{\text{ORIGINAL}}$$

PERCENT

EQUATIONS AND INEQUALITIES

CHEAT SHEET - A

Name _____

Date _____ Pd _____

SOLVING EQUATIONS

Use **INVERSE OPERATIONS** to **UNDO** the equation.

- undo addition or subtraction $6x+7=31$
- undo multiplication or division $6x=24$
- isolate the variable $x=4$
- check your work $6(4)+7=31$

inequalities

SAME STEPS as **SOLVING EQUATIONS!**

- When dividing by a negative number, flip the inequality symbol.
- To check your work, choose a value that is within the constraints of the inequality and plug in the number.
- If it is correct, then you should get a true statement.

GRAPH the inequality statement on a number line to represent **THE POSSIBLE SOLUTIONS**.

● VALUE IS INCLUDED ○ VALUE IS NOT INCLUDED

graphing inequalities

CHECK ✓

$$-\frac{1}{2}x - 5 > 25 \quad -\frac{1}{2}(-80) - 5 > 25$$

$$-\frac{1}{2}x > 30 \quad -\frac{1}{2}(-80) > 30$$

$$x < -60 \quad 40 > 30$$

INEQUALITY VOCABULARY

- Remember that each term can represent a different inequality symbol when writing inequalities.

<	≤	>	>	=
<ul style="list-style-type: none"> • less than • is fewer than • is smaller than • below 	<ul style="list-style-type: none"> • less than or equal to • maximum • at most • is not more than • is not greater than 	<ul style="list-style-type: none"> • greater than or equal to • minimum • at least • is not less than • is not smaller than 	<ul style="list-style-type: none"> • greater than • is more than • is larger than • above 	<ul style="list-style-type: none"> • equal • is • same

ORIGINAL EXPRESSION	PROPERTY	EQUIVALENT EXPRESSION
$8 + 0$	IDENTITY	8
$6 \cdot 3 \cdot 2$	COMMUTATIVE	$3 \cdot 2 \cdot 6$
$6 + (3 + 2)$	ASSOCIATIVE	$(6 + 3) + 2$
$8(x + 7)$	DISTRIBUTIVE	$8x + 56$

PROPERTIES OF OPERATIONS RESULT IN EQUIVALENT EXPRESSIONS

The **RECIPROCAL** of a number results in a

PRODUCT OF 1.

$$\frac{5}{6} \cdot \frac{6}{5} = 1$$

FLIP

PROPERTIES OF OPERATIONS